

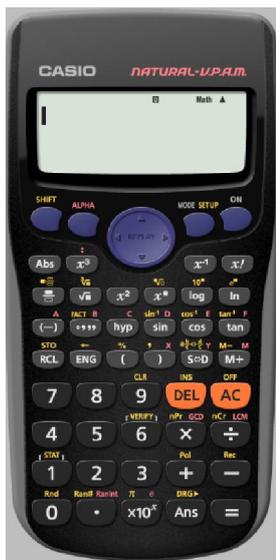
# Sequences

*This resource was written by Derek Smith with the support of CASIO New Zealand. It may be freely distributed but remains the intellectual property of the author and CASIO.*

A sequence is a list of numbers; the numbers in this list are called 'terms' of the sequence and are linked to each other by a mathematical rule (formula).

A series is when you add up the terms of a sequence; For instance,  $\langle 1, 2, 3, 4, \dots \rangle$  is a sequence, with terms '1', '2', '3', '4', etc.. The terms of a sequence are usually named ' $a_n$ ', with the subscripted letter ' $n$ '. So, the second term of a sequence is named ' $a_2$ ', and ' $a_{12}$ ' would be the twelfth term.

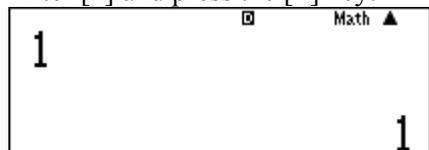
Partial sums ( $S_n$ ) indicate the adding together of terms. For example, the 4<sup>th</sup> partial sum ( $S_4$ ) of the series above is the sum ' $1 + 2 + 3 + 4$ ', and equals 10. So,  $S_n = 10$ .



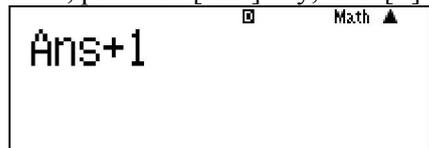
Set the up calculator to **COMP MODE**.



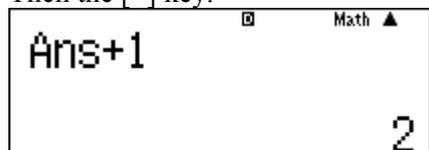
**Example 1:** Generate the sequence  $\langle 1, 2, 3, 4, \dots \rangle$   
Enter [1] and press the [=] key.



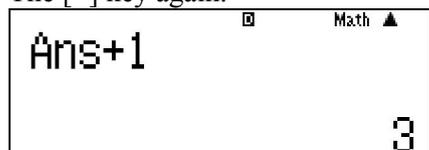
Now, press the [Ans] key, then [+] [1]



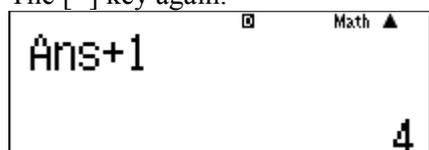
Then the [=] key.



The [=] key again.

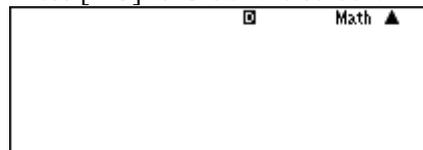


The [=] key again.

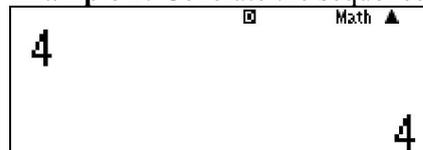


And [=] key again...

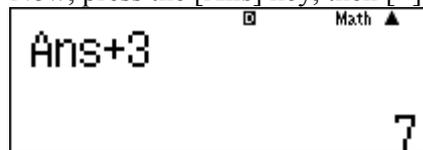
Press [AC] to **Clear** the screen.



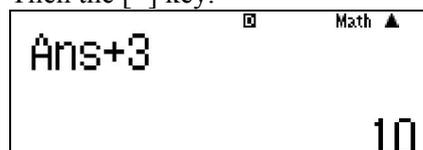
**Example 2:** Generate the sequence  $\langle 4, 7, 10, 13, \dots \rangle$



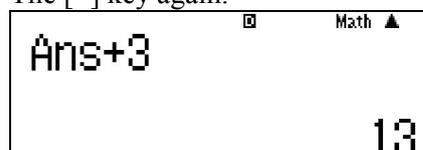
Now, press the [Ans] key, then [+] [3]



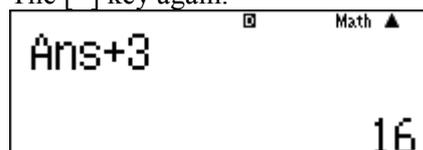
Then the [=] key.



The [=] key again.

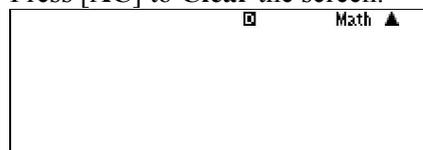


The [=] key again.

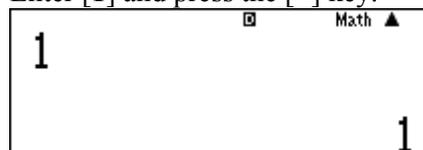


And [=] key again...

Press [AC] to **Clear** the screen.

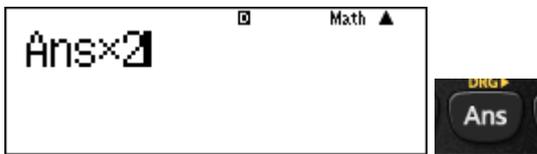


**Example 3:** Generate the sequence  $\langle 1, 2, 4, 8, \dots \rangle$   
Enter [1] and press the [=] key.

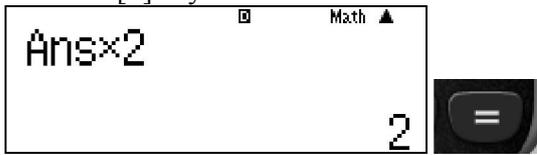


Now, press the [Ans] key, then [×] [2]

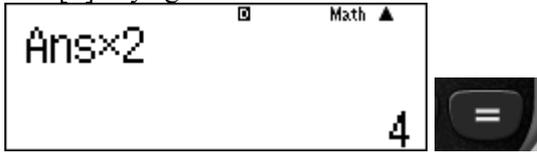




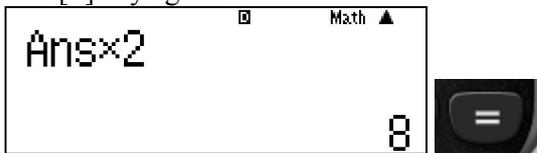
Then the [=] key.



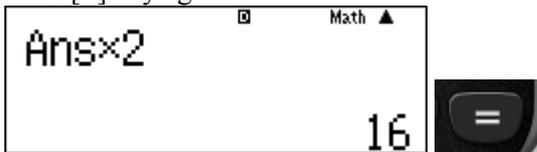
The [=] key again.



The [=] key again.

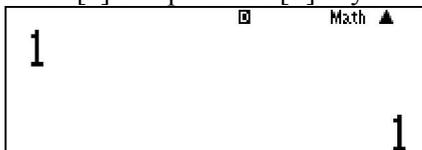


And [=] key again...



**Example 4:** Generate the sequence  $\langle 1, -2, 4, -8, \dots \rangle$

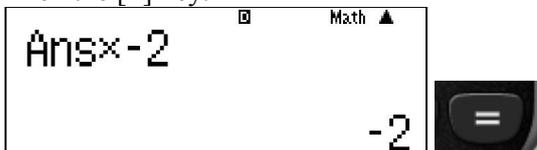
Enter [1] and press the [=] key.



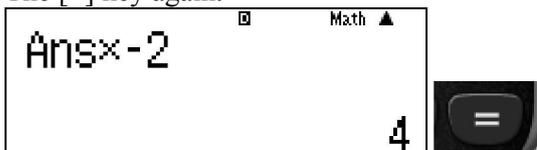
Now, press the [Ans] key, then [ $\times$ ] [-2]



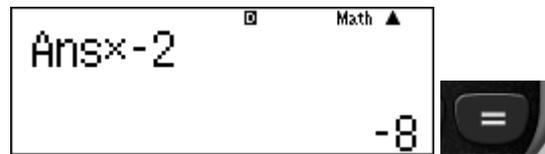
Then the [=] key.



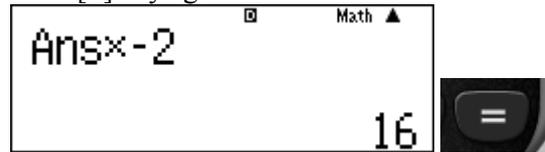
The [=] key again.



The [=] key again.



And [=] key again...



An **arithmetic** sequence is a sequence with the difference between two consecutive terms constant. The difference is called the common difference,  $d$ . In general,  $a$  is the first term of the sequence and  $n$  is the term number. This is adding (or subtracting) as illustrated in Examples 1 and 2.

The general rule in generating each term is:

$$a_n = a + (n - 1)d$$

A **geometric** sequence is a sequence with the ratio between two consecutive terms constant. This ratio is called the common ratio,  $r$ . In general,  $a$  is the first term of the sequence and  $n$  is the term number.

This is multiplying (or dividing) as illustrated in Examples 3 and 4.

The general rule in generating each term is:

$$a_n = ar^{(n-1)}$$

**Practice for arithmetic sequences:**

Find the next three terms:

3, 10, 17, 24, 31, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

Find the 25<sup>th</sup> term:

53, 50, 47, 44, 41, ... \_\_\_\_\_

Find the 20<sup>th</sup> term:

25, 40, 55, 70, 85, ... \_\_\_\_\_

Find the 75<sup>th</sup> term:

88, 81, 74, 67, 60, ... \_\_\_\_\_

Antonio received a bonus of \$50 for working the day after Thanksgiving, plus his regular wage of \$9.45 an hour. If his total wages for the day were \$135.05, how many hours did he work?

**Practice for geometric sequences:**

Find the next three terms:

128, 64, 32, 16, 8, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_.

Find the 9<sup>th</sup> term:

0.01, 0.1, 1, 10, 100, ... \_\_\_\_\_

Find the 7<sup>th</sup> term:

1, 6, 36, 216, 1,296, ... \_\_\_\_\_

Find the 11<sup>th</sup> term:

1, -2, 4, -8, 16, ... \_\_\_\_\_

Wikitoria makes \$18.50 per hour. Every three months, she is eligible for a 2% raise. How much will she make, an hour, in 2 years time, if she gets a raise every time she is eligible?